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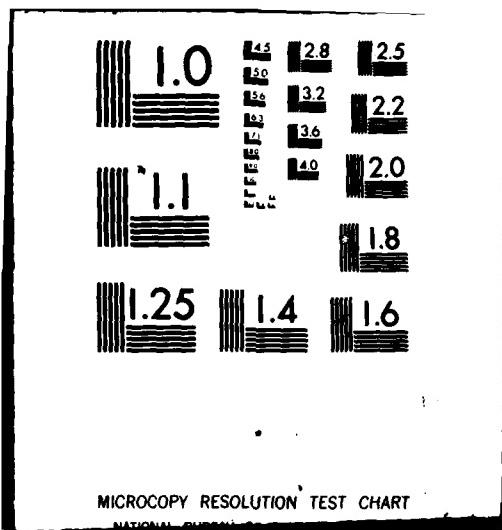
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## ELECTRICAL PROPERTIES OF HEATED DIELECTRICS (U)

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### INTRODUCTION

For the past decade there has been a great deal of work devoted to understanding the pyroelectric and piezoelectric mechanisms in several of the high polymers, most notably in the material poly(vinylidene fluoride), PVF<sub>2</sub>. At the present time PVF<sub>2</sub> has the highest piezo-pyroelectric response among polymeric materials. Since the early work on the pyroelectric properties of PVF<sub>2</sub> by Nakamura and Wada (1) and Bergman et al (2), considerable effort has been expended in attempts to improve the pyroelectric response of this polymer for numerous practical applications including reflectivity measurements (3), a photocopy process (4), infrared radiation detection (5),(6), thermal imaging with a pyroelectric vidicon (7),(8), intrusion and fire detection (9), and non-linear optical devices (2). In spite of this intense activity the nature of the mechanism (or mechanisms) of pyroelectricity in PVF<sub>2</sub> is not fully understood (10),(11). To a large extent much of the confusion surrounding the understanding of the electrical behavior of this important material is due to ambiguous results associated with the interpretation of different measurement techniques used to explore its properties.

Several techniques have been used in the past to accurately determine the pyroelectric properties of dielectric materials (4),(12),(13), (14). Some of these techniques have been reviewed recently regarding their usefulness in the characterization of pyroelectric materials intended for use as infrared radiation detectors or as targets in a pyroelectric vidicon (PEV) (8). As radiation detectors, pyroelectric materials must exhibit a current response that is completely reversible and reproducible when subjected to small temperature changes.

There are numerous materials which exhibit a large non-pyroelectric current response (non-reversible) when they are heated (15). There are also many materials which are capable of exhibiting both non-pyroelectric and pyroelectric responses simultaneously when they are heated. Since only the reversible pyroelectric current contributes to infrared response, it is obvious that any technique used to evaluate such materials for use as

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infrared radiation detectors must provide the capability for distinguishing the current contributions associated with pyroelectric behavior and those associated with non-pyroelectric behavior and to permit the determination of their individual magnitudes.

Typically PVF<sub>2</sub> film is only weakly pyroelectric in the as received condition. When PVF<sub>2</sub> is subjected to an applied electric field (poling), significant pyroelectric response can be generated in the film and this response may be further enhanced or degraded by additional or simultaneous thermal and mechanical treatments (stretching). A recent review article on PVF<sub>2</sub> by Das-Gupta (16) discusses these poling techniques and their subsequent effects on the structure, pyroelectric behavior, and the possible models to explain this behavior.

It has been reported (8),(17) that the first thermal cycle of a poled PVF<sub>2</sub> sample will yield a predominantly non-pyroelectric current (thermally stimulated current or conductivity, TSC) (15) as a function of temperature and that the second and subsequent thermal cycles yield a reversible pyroelectric current (4). The shape of the first thermal cycle current curve depends upon the poling procedure (18). Here we describe a new method which allows the analysis and evaluation of electric currents such as pyroelectric currents and thermally stimulated currents arising from heated dielectric materials. This method can be applied to materials that exhibit only pyroelectric currents, materials that exhibit only non-pyroelectric currents, or materials that exhibit a combination of the two types of currents. Pyroelectric current is directly proportional to the derivative of temperature with respect to time. Non-pyroelectric current, in general, is either constant or within small temperature intervals nearly proportional to the temperature. These assumptions have been verified (19),(20) mathematically in certain temperature and frequency ranges and experimentally for a number of different dielectric materials, several of which will be discussed here. Poly(vinylidene fluoride) has been selected as one of the materials since it is an important material from an applications point of view. It also lends itself well to demonstrating the strength and validity of the following treatment and measurements.

#### THEORY

For the present we assume that non-pyroelectric currents can be represented by

$$i_n = i_0 + RT, \quad [1]$$

where  $i_0$  is a constant, non-pyroelectric, temperature independent current. The term  $RT$  is also non-pyroelectric, but it increases linearly with temperature  $T$ ;  $R$ , being a temperature coefficient. It

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has been shown previously (20) that within small temperature intervals TSC can be approximated by this form. Equation [1] is used because it is general and applies to any non-pyroelectric current that may be present.

The pyroelectric current can be written as (12),(14)

$$i_p = pA \frac{dT}{dt} , \quad [2]$$

where  $p$  is the pyroelectric coefficient  $A$ , the sample area and  $dT/dt$  the time derivative of the temperature.

In a material where both currents are present the total current can be written as

$$i_T = i_0 + RT + pA \frac{dT}{dt} . \quad [3]$$

In typical measurements of TSC and pyroelectric current, the sample temperature is  $T_o + bt$ , where  $T_o$  denotes the initial absolute temperature of the sample and  $bt$  is the temperature change introduced when the sample is heated at a constant rate  $b$  for a time  $t$  (14),(21),(22). If, in addition to this normal method of heating, a small sinusoidal temperature component of amplitude  $T_1$  and angular frequency  $\omega$  is imposed on the sample, the temperature becomes

$$T = T_o + bt + T_1 \sin(\omega t) . \quad [4]$$

The total current from the sample under these heating conditions can now be written as a sum of an ac-current and a dc-current as

$$i_T = [i_0 + R(T_o + bt) + pAb] + [RT_1 \sin(\omega t) + pAT_1 \omega \cos(\omega t)] . \quad [5]$$

For sufficiently large frequencies the term  $Rbt$  is nearly constant during the period of a heat wave and is therefore included in the dc-current term. It is important to note that the term  $RT_1 \sin(\omega t)$ , which is in phase with the sinusoidal component of temperature, comes from the non-pyroelectric part of Eq. [3]. On the other hand, the term  $pAT_1 \omega \cos(\omega t)$  comes from the pyroelectric component of Eq. [3] and the resulting current precedes the sinusoidal temperature wave by  $90^\circ$ . Thus ac-components of non-pyroelectric currents are in phase with the temperature whereas ac-components of pyroelectric currents precede the temperature by  $90^\circ$ . The ac portion of the current given by Eq. [5] can be written as

$$i_{ac} = i_1 \sin(\omega t + \theta) , \quad [6]$$

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$$i_1 = (i_n^2 + i_p^2)^{1/2}, \quad [7]$$

$$i_n = RT_1, \quad [8]$$

$$i_p = pAT_1\omega, \quad [9]$$

$$\theta = \tan^{-1}(i_p/i_n) = \tan^{-1}(pA\omega/R). \quad [10]$$

The amplitudes of the non-pyroelectric and pyroelectric currents are given by  $i_n$  and  $i_p$  respectively. The amplitude of the ac-current  $i_1$  therefore depends upon the amplitude of both the pyroelectric current and the non-pyroelectric current. An examination of the amplitude of the ac-component  $i_1$  is not sufficient to determine if the current is pyroelectric or non-pyroelectric. The phase difference  $\theta$  between the temperature and current waves must be determined to establish which type of current is present. For example, in a purely pyroelectric material  $i_n$  will be zero and  $\theta = 90^\circ$ , and for a material with no pyroelectric response  $i_p$  will be zero and  $\theta = 0^\circ$ . When a material exhibits both types of currents the extrema of the ac-current precede the extrema of the temperature by a phase angle somewhere between  $0^\circ$  and  $90^\circ$ . Thus if we measure the phase of the ac-current with respect to the temperature wave, we can determine if the current is pyroelectric or non-pyroelectric and we can use Eq. [7] and [10] to compute the fraction of current associated with each effect. These components are:

$$i_p = i_1 \sin(\theta), \quad [11]$$

$$i_n = i_1 \cos(\theta). \quad [12]$$

It has been shown that the TSC arising from numerous relaxation processes has the following time and temperature dependence (15),(21),(22).

$$i_b = C \exp \left[ \frac{-E}{kT} - B \int_0^t \exp \left( \frac{-E}{kT} \right) dt \right]. \quad [13]$$

where the constants C and B depend on the origin of the TSC. This relation assumes a single relaxation time of the form  $\tau = \tau_0 \exp(E/kT)$  where  $\tau_0$  is a constant, E is an activation energy, and k is Boltzmann's

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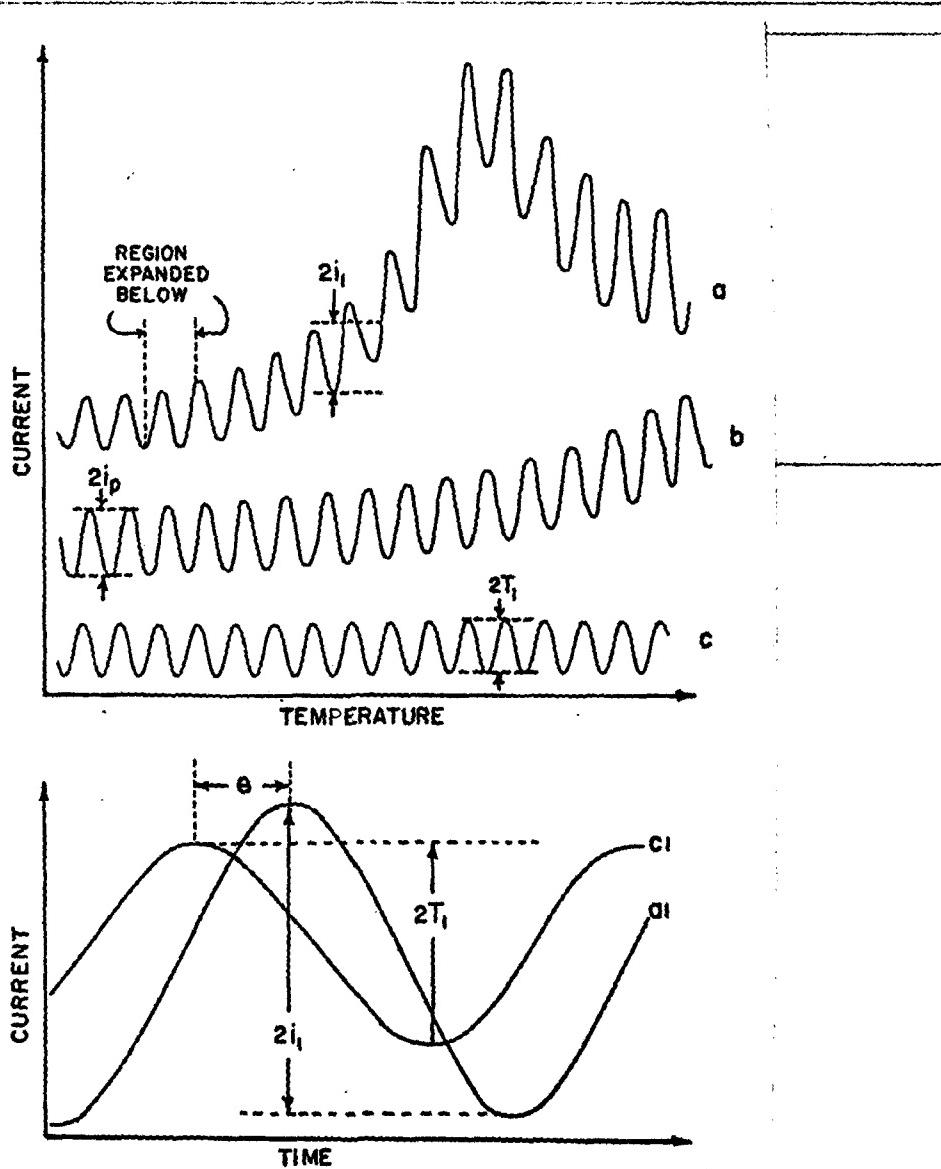


Figure 1. Sketch of actual data for a pyroelectric material such as  $\text{PVF}_2$ . A small section of the current versus temperature data is expanded in the lower set of curves to illustrate the observed phase shift,  $\theta$ . Curve (a) represents the current arising from a first thermal cycle, curve (b) is the current arising from subsequent thermal cycles, and curve (c) is the ac-temperature wave.

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constant. This assumption is consistent with our observations of TSC curves of PVF<sub>2</sub> samples rested equal lengths of time (18). There is some temperature  $T_m$  at which maximum TSC occurs for a sample heated at a constant rate  $b$ , ( $T = T_0 + bt$ ) determined by maximizing Eq. [13] with respect to  $t$ . The value of  $T_m$  depends strongly upon the rest time after poling and in general the TSC decreases sharply for  $T > T_m$  (18).

It has been previously shown (20) that within small temperature intervals the TSC given by Eq. [13] is a linear function of temperature for a constant heating rate of the form  $T = T_0 + bt$ . For temperatures of the form given by Eq. [4]  $i_b$  is non-pyroelectric and can be represented by Eq. [1]. Where the period of the sinusoidal temperature wave and the heating rate can be chosen such that  $i_0$  and  $R$  change very little during several periods of the heat wave (20). The value of  $R$  is then expressed as:

$$R = \frac{i_b E}{k(T_0 + bt)^2} . [14]$$

It is useful to examine the influence of the temperature dependence of  $R$  on the magnitude and phase of the ac-current. We can rewrite the expression for the amplitude of the ac-component  $i_1$  in terms of the pyroelectric and non-pyroelectric current amplitudes given by Eqs. [8] and [9].

$$i_1 = \left[ \left( \frac{i_b E T_1}{k(T_0 + bt)^2} \right)^2 + (p A \omega T_1)^2 \right]^{1/2} , [15]$$

where  $R$  has been written in the form given by Eq. [14]. Since  $i_b$  has the characteristic TSC dependence on temperature, the non-pyroelectric amplitude and therefore the ac-component  $i_1$  will increase as  $i_b$  increases to its maximum at  $T_m$ . As the temperature is increased beyond  $T_m$ ,  $i_b$  decreases to zero and the first term in Eq. [15] vanishes and  $i_1$  is then equal to the amplitude of the pyroelectric current. The change in  $i_b$  with temperature does not influence  $i_1$  but it does influence the phase angle. Since  $\theta$  decreases as  $R$  increases,  $\theta$  will reach a minimum when  $i_b$  is a maximum at the temperature  $T_m$ . The amplitude and phase of the ac-current,  $i_1$ , and  $\theta$ , can be measured directly and compared with computed values.

To better understand this procedure, Fig. 1 is presented. It represents an actual display of data taken on a sample that exhibits both TSC and pyroelectric response such as a PVF<sub>2</sub> sample might have. This figure is used to identify the various parameters associated with the theory and to demonstrate how to extract the information necessary to

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apply the theory from a typical sample of recorded data.

When a sample is thermally cycled for the first time curves (a) and (c) are recorded concurrently. Curve (a) is the total current, pyroelectric and non-pyroelectric, released from the sample as it is heated under the conditions given by Eq. [4]. Curve (c) is a recording of only the sinusoidal portion of the applied temperature,  $T_1 \sin(\omega t)$ , which oscillates about  $(T_0 + bt)$ . For each subsequent thermal cycle the current, curve (b), and a new curve (c) are recorded so that phase measurements can be made. It is important to note that curve (a) as shown in Fig. 1 is representative of those obtained on PVF<sub>2</sub>. In materials which exhibit only pyroelectric response curves (a) and (b) will be identical. At selected temperatures ( $T_0 + bt$ , see Eq. [4]) throughout the thermal cycle, usually every 10°C, new curves (c1) and (a1) are recorded to graphically magnify the phase difference between them.

The analysis of data is simplified by noting that A and k are constants,  $\omega$  and  $T_1$  are fixed by the temperature wave period, and the quantity  $(T_0 + bt)$  is just the measurement temperature at some time t during the thermal cycle. The values of the three quantities remaining in the expression for the ac-current amplitude,  $i_b$ , E, and p along with the phase difference can be extracted from the data as follows: the pyroelectric coefficient, p, can be estimated using second run current dc-values (18). This, together with the values of A,  $T_1$ , and  $\omega$ , provides a computed value for the amplitude of the ac-pyroelectric current component  $pAT_1\omega$ . If the dc-component of the curve (a) is measured and the dc-component of curve (b) is subtracted off (18), the resulting current  $i_b$  can be subjected to the usual (21), (22) TSC analysis and a determination of the activation energy can be made. The amplitude of the non-pyroelectric ac-current can be computed from Eq. [8]. The values  $i_n$  and  $i_p$  can now be used to compute  $i_1$  and  $\theta$  which may then be compared with the measured values.

## EXPERIMENTAL RESULTS

We have examined two ferroelectric materials in the temperature range 0°C to 80°C: triglycine sulfate (TGS),  $(\text{NH}_2\text{CH}_2\text{COOH})_3 \cdot \text{H}_2\text{SO}_4$ , and lithium tantalate, LiTaO<sub>3</sub>. Samples of each material were prepared from 50 μm thick wafers having circular nichrome electrodes deposited on both sides so that they formed capacitors with an area of 0.6 cm<sup>2</sup>. Fine wire leads were silver-epoxied to non-overlapping tabs extending from the circular electrodes and the samples were poled at room temperature with dc-electric fields of  $10^3 - 10^4$  V/cm for both materials.

TGS exhibits Curie behavior in this temperature range at  $\sim 49^\circ\text{C}$  but LiTaO<sub>3</sub> does not since it is a high-temperature ferroelectric with a Curie temperature  $T_c \approx 618^\circ\text{C}$  (23), (24). Figure 2 shows the measured ac- and dc-components of pyroelectric current for lithium tantalate as a function of temperature from 0°C to 80°C for 5, 10, 20, 50, 100, and

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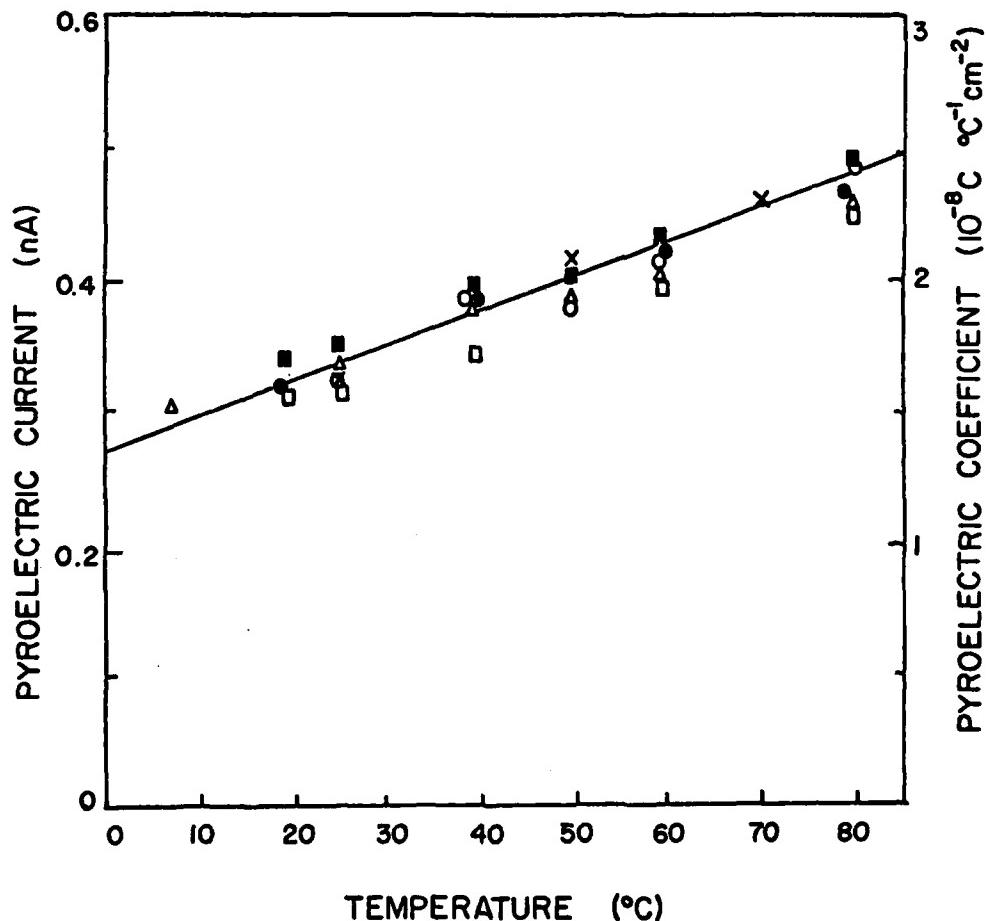


Figure 2. Pyroelectric current as a function of temperature for  $\text{LiTaO}_3$ . The values of the pyroelectric coefficients associated with these currents are also shown. Here the straight line is the measured dc-value of the pyroelectric current and the ac-values are for different temperature wave periods as: (5 sec-X), (10 sec-■), (20 sec-□), (50 sec-△), (100 sec-●), and (200 sec-○).

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200 sec temperature wave periods. The value of the pyroelectric coefficient for  $\text{LiTaO}_3$  at  $25^\circ\text{C}$  is in agreement with the values reported by other workers (14), (24), (25),  $1.76 \times 10^{-8} \text{ C/cm}^2$  to  $1.9 \times 10^{-8} \text{ C/cm}^2 \text{ }^\circ\text{C}$ .

The pyroelectric coefficients for TGS obtained from the measured ac and dc-components of the current are compared in Fig. 3. The value of the pyroelectric coefficient,  $p = 3 \times 10^{-8} \text{ C/cm}^2 \text{ }^\circ\text{C}$  obtained at  $23^\circ\text{C}$  agrees well with the values reported by others, (25), (26),  $2.8 \times 10^{-8} \text{ C/cm}^2 \text{ }^\circ\text{C}$  and  $2-3.5 \times 10^{-8} \text{ C/cm}^2 \text{ }^\circ\text{C}$ . The markedly different pyroelectric response curves for TGS and  $\text{LiTaO}_3$  shown in Figs. 2 and 3 stem from the fact that TGS exhibits Curie behavior in the measurement temperature range. Even though the measured pyroelectric response of TGS varies nearly two orders of magnitude and  $\text{LiTaO}_3$  varies only slightly, there is good agreement between the ac and dc-current components for both materials.

The phase difference for these two materials is determined graphically as described earlier and these values are shown in Fig. 4 from  $0^\circ\text{C}$  to  $80^\circ\text{C}$ . The  $\pi/2$  phase shifts at all temperatures indicate that  $i_1$  has no non-pyroelectric ac-component and thereby confirms that the materials are purely pyroelectric.

Hundreds of  $\text{PVF}_2$  samples were prepared from 6 m thick biaxially oriented film and electrodeed to form capacitors in the same manner as the ferroelectric materials. These samples were then poled at relatively high fields,  $1.3 \times 10^6 \text{ V/cm}$ , at room temperature. This procedure assured that the samples were well poled as described by Day et al (27).

The currents from these samples were recorded as a function of temperature from  $0^\circ\text{C}$  to  $80^\circ\text{C}$  at a  $2^\circ/\text{min}$  heating rate in the presence of a small low-frequency sinusoidal temperature wave. Each specimen was measured several times and data similar to that depicted in Fig. 1 was obtained for each sample. Pyroelectric coefficients obtained at room temperature of  $1 \times 10^{-9} \text{ C/cm}^2 \text{ }^\circ\text{C}$  are in good agreement with those of a number of other workers for similarly poled samples (27), (28). Following the analysis procedure outlined earlier, the phase shifts for the first thermal cycles of identically poled and rested samples are shown in Fig. 5 for temperature wave periods of 5, 20, 50, and 100 seconds.

Note that in these curves the position of the maximum phase shift from  $\pi/2$  corresponds to the maximum value of  $i_b$  (TSC current) as can be seen from Eqs. [10] and [14]. The position of  $T_m$  for well-polled samples prepared at room temperature depends on the rest time,  $t_r$ , through the phenomenological relationship  $T_m = 309 + 6.5 \log(t_r)$  which has been extracted from the data of Ref. (18). For samples rested three days,  $t_r = 72$  hours,  $T_m$  corresponds to  $\sim 47^\circ\text{C}$  as indicated in the phase-shift data of Fig. 5. The absolute value of the phase angle is dependent upon the temperature-wave-period as seen from Eq. [10] and is also in evidence in Fig. 5.

Second and subsequent thermal cycles yield  $\pi/2$  phase shifts for these same samples indicating reversible and reproducible pyroelectric behavior. Figure 6 shows a plot of the computed and measured phase.

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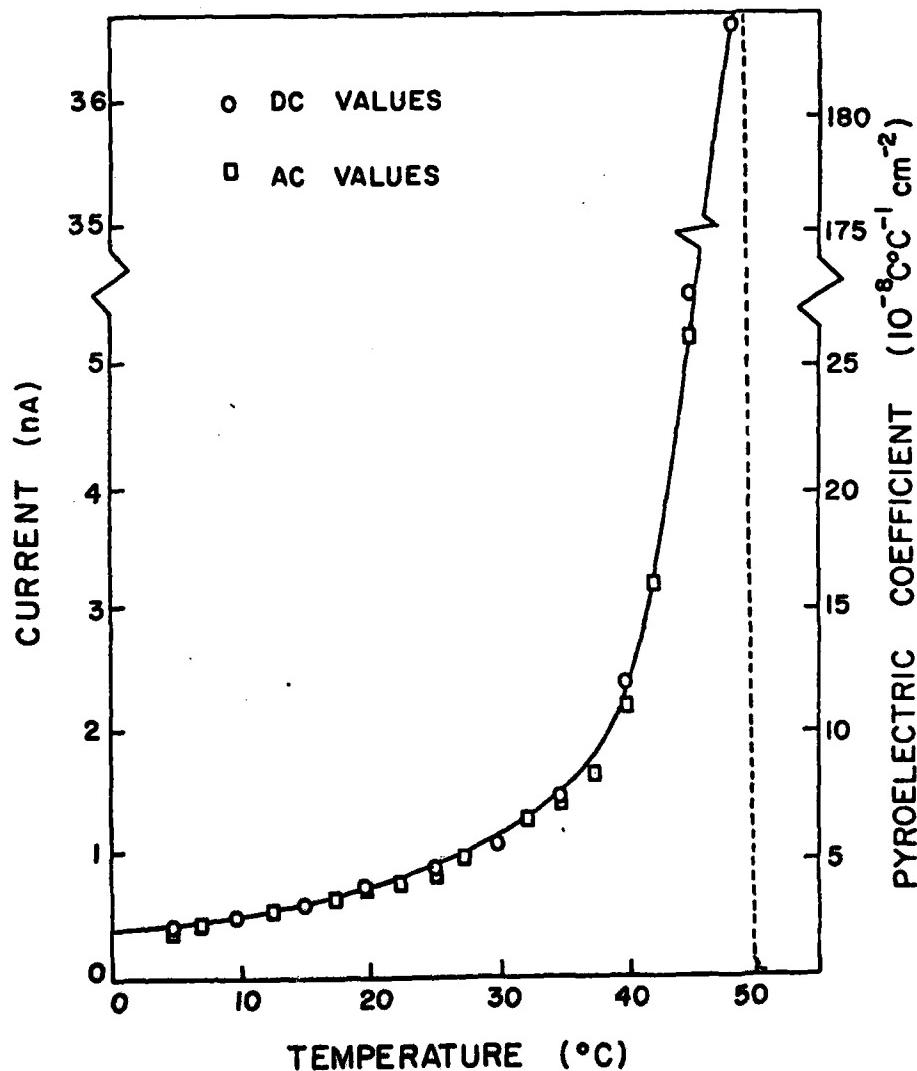


Figure 3. Measured ac and dc-pyroelectric current and corresponding pyroelectric coefficients for triglycine sulfate for a 20-second temperature wave period.

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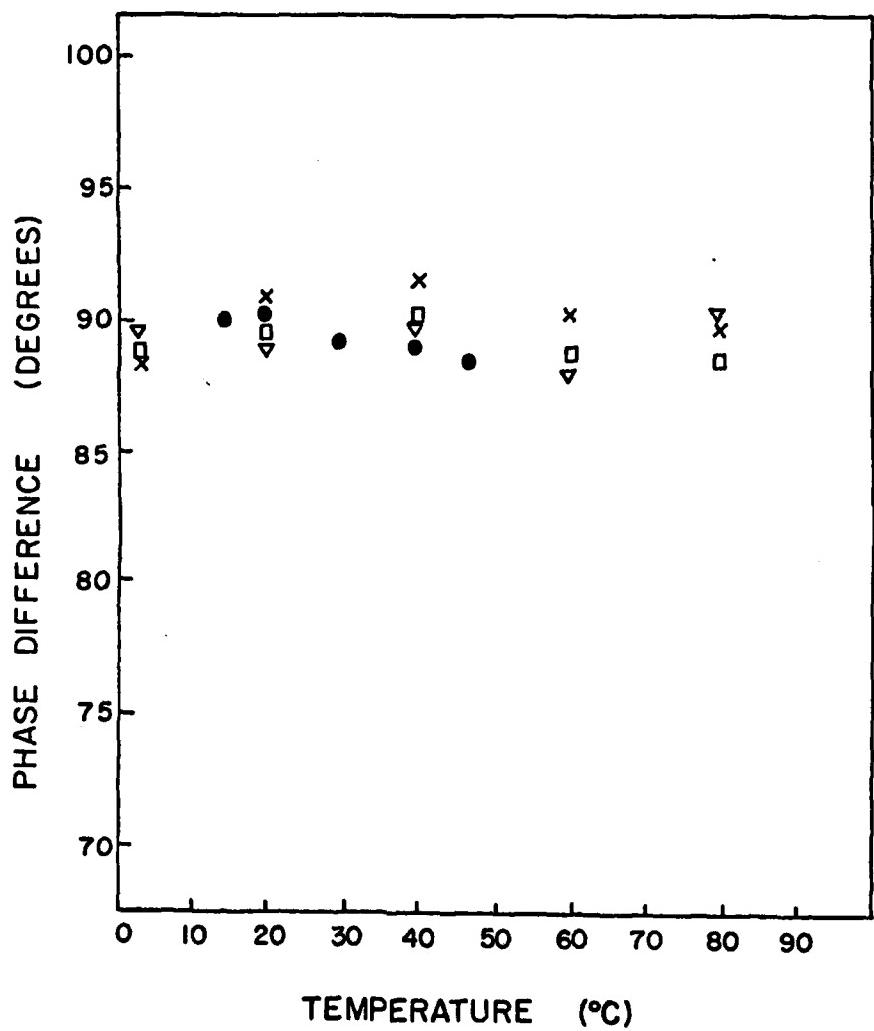


Figure 4. Phase difference between measured current and applied ac-temperature wave as a function of temperature for TGS (20 sec-●) and LiTaO<sub>3</sub> (5 sec-X), (50 sec-□), and (200 sec-△).

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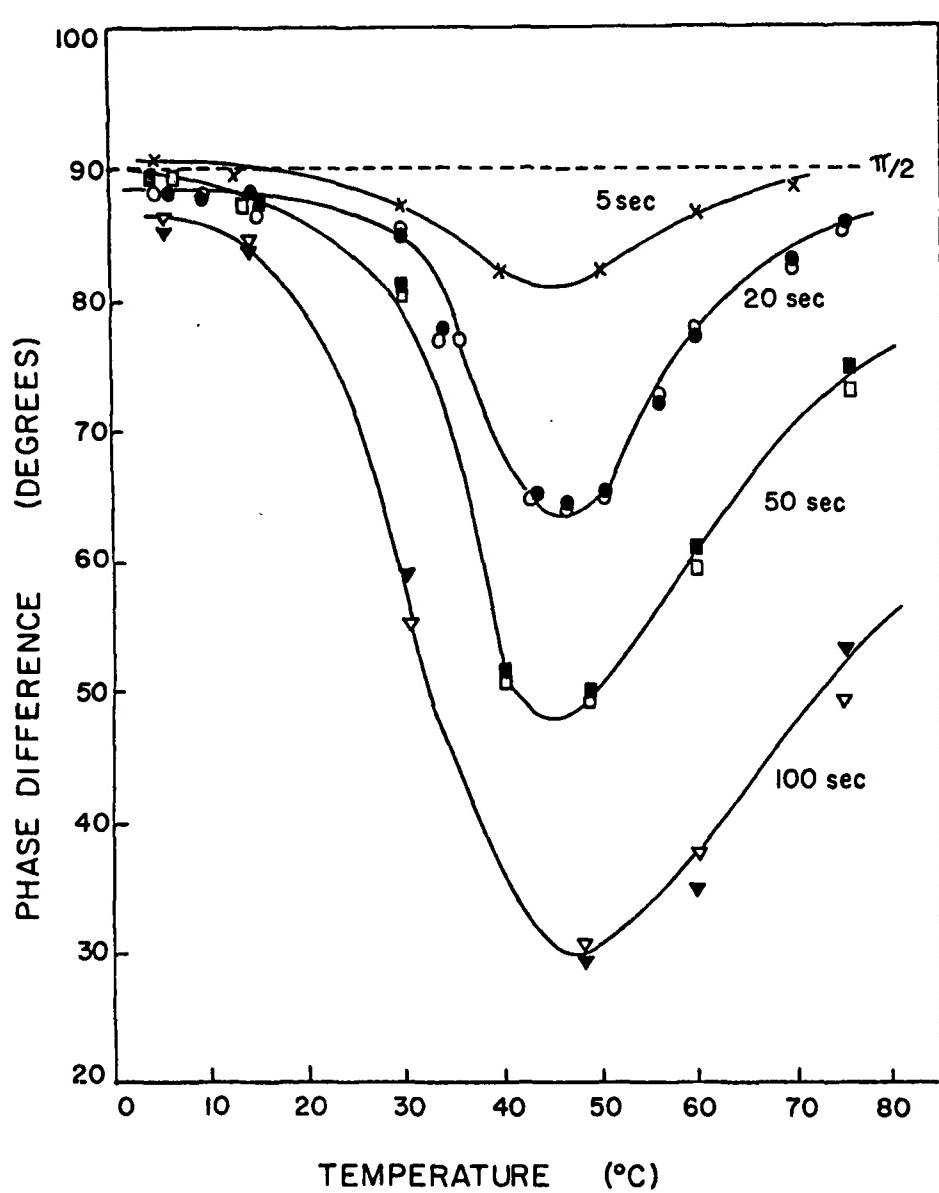


Figure 5. First thermal cycle phase difference between measured current and ac-temperature waves as a function of temperature for identically poled PVF<sub>2</sub> samples. Here solid points are computed from Eq. [10] and the open points are determined graphically from the data.

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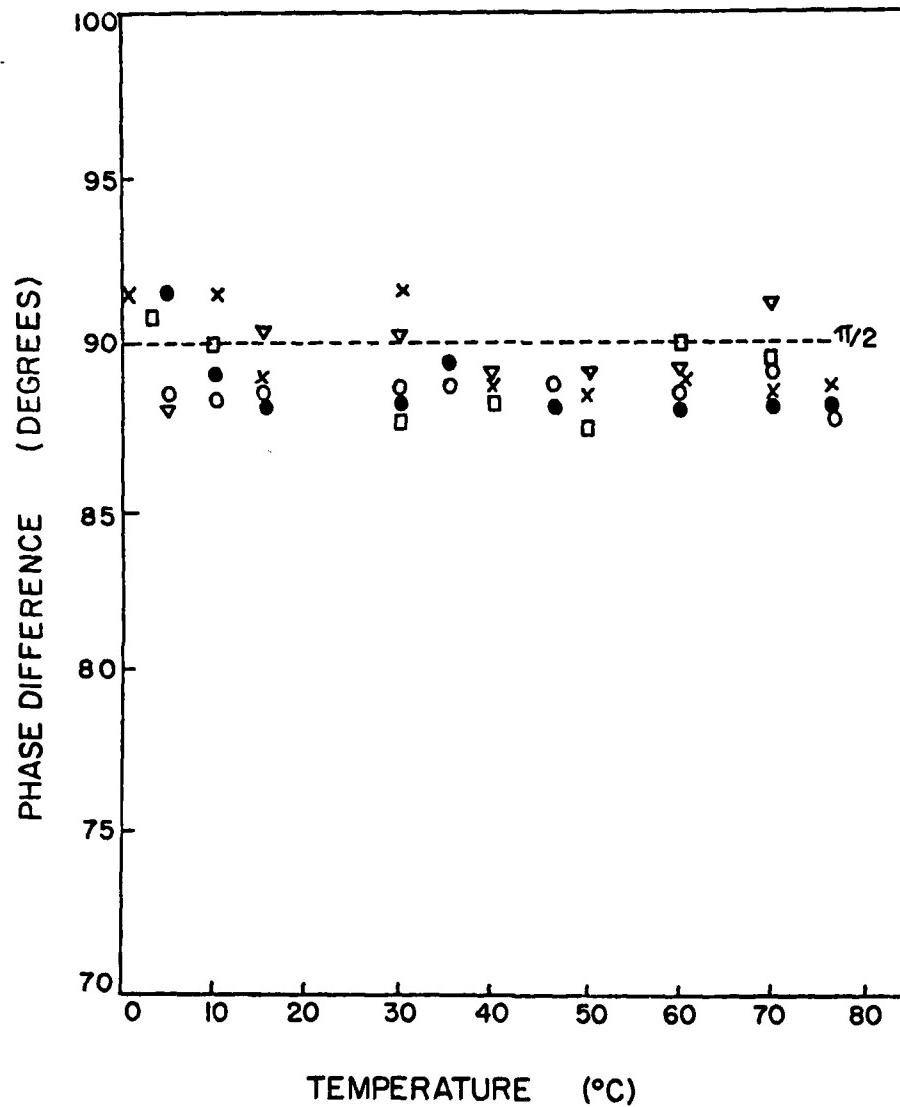


Figure 6. Computed (solid points) and measured (open points) phase differences of the second and third thermal cycles for identically poled PVF<sub>2</sub> samples. Here (20 sec-X), third run; (20 sec<sup>2</sup>-○), (5 sec-△), and (50 sec-□), all second run; and (20 sec-●), computed second run.

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shifts of the second and third thermal cycles for temperature wave periods of 5, 20, and 50 seconds.

### CONCLUSIONS

A method has been described which allows one to analyze complicated currents emanating from warmed dielectrics. This technique is easily applied for temperature waves of certain amplitude and frequency limits and permits an accurate assessment of dielectric materials being examined for specific applications, such as infrared detectors or vidicon targets, where it is necessary to know the current magnitude and relaxation properties as a function of temperature and temperature changes.

The low-frequency temperature wave method is a direct dynamic measurement of the pyroelectric coefficient. This method eliminates the need for measurements of specific heats, dielectric constants, and radiation absorption coefficients as well as identifying the effects due to irreversible currents which occur when samples are heated at a constant rate.

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